

FIGURE 1

**TITLE: SPECIFICATION BASED DETECTION AND REPAIR OF
ERRORS IN DATA STRUCTURES**

Inventors: Brian C. Demsky, et al.

Filed: November 26, 2003 MIS-00401

Agent: Anne E. Saturnelli Reg. No.: 41,290

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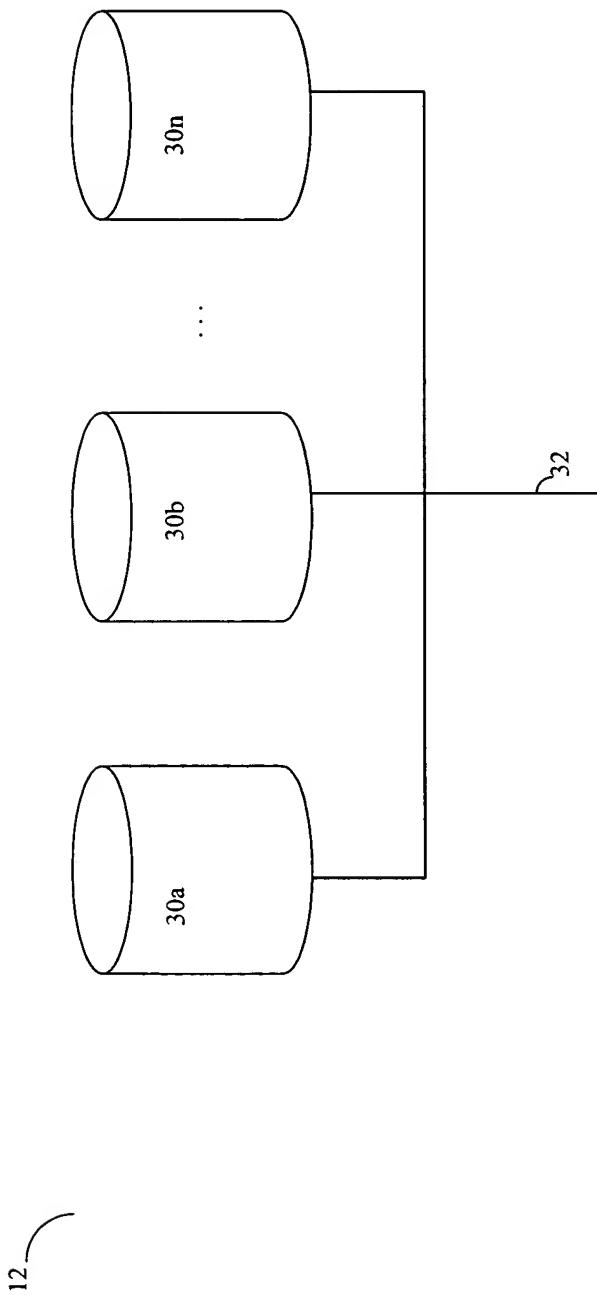


FIGURE 2

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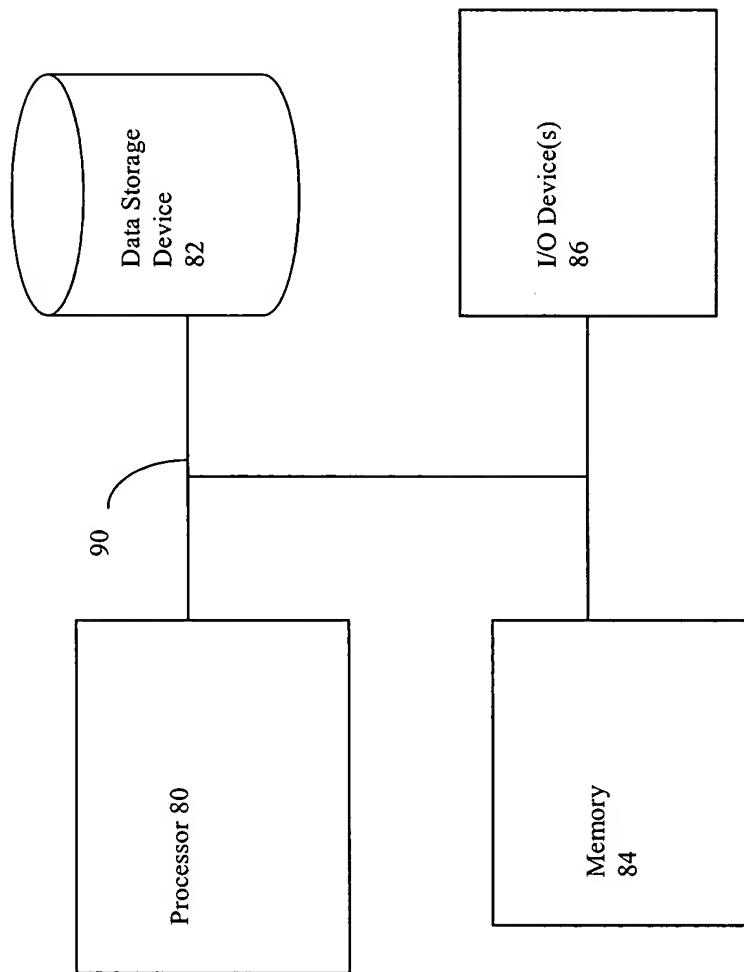


FIGURE 3

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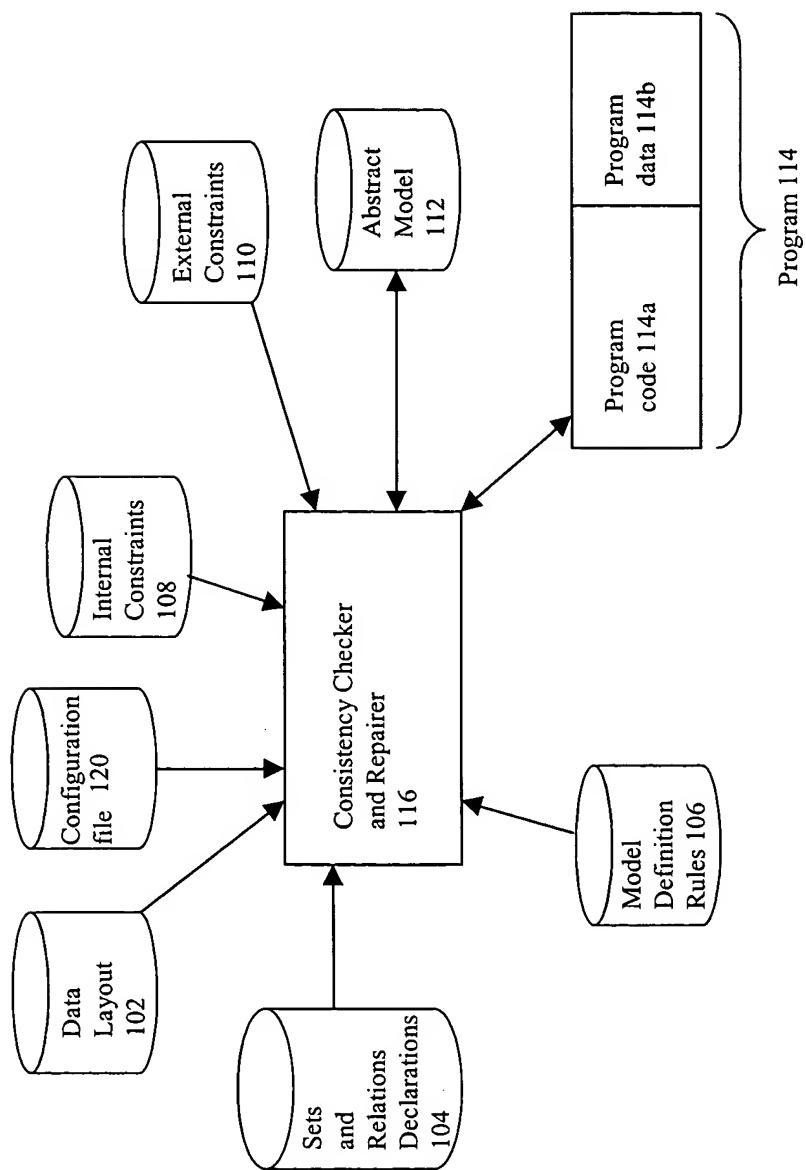


FIGURE 4

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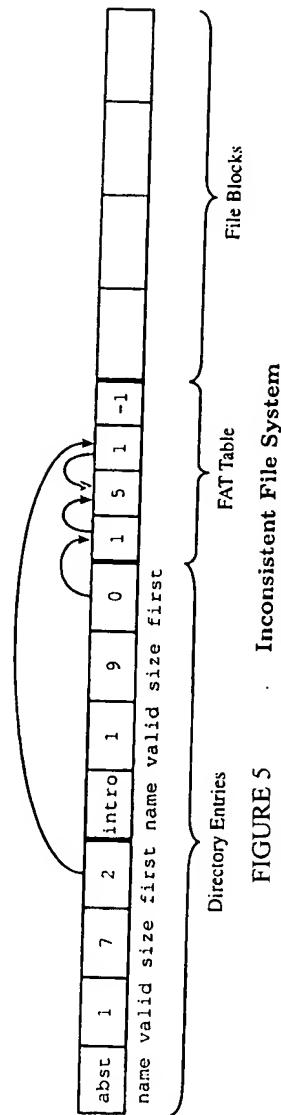


FIGURE 5 Inconsistent File System

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```
structdefn := struct structurename
              (subtypes structurename) {fielddefn*}

fielddefn := type field; | reserved type; |
            type field[E]; |
            reserved type[E];

type := boolean | byte | short | int | structurename |
        structurename *

E := `V | number | string | E.field |
    E.field[E] | E - E | E + E | E/E | E * E
```

FIGURE 6 Structure Definition Language

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```
struct Entry {  
    byte name[Length];  
    byte valid;  
    int size;  
    int first;  
}  
  
struct Block { data byte[BlockSize]; }  
  
struct Disk {  
    Entry table[NumEntries];  
    int FAT[NumBlocks];  
    Block block[NumBlocks];  
}
```

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FIGURE 7 . Structure Declarations

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125 {
set S of T : Partition S_1, \dots, S_n
relation R : $S_1 \rightarrow S_n$

FIGURE 8A

126 {
set blocks of integer : partition used | free
relation next : used \rightarrow used;

FIGURE 8B

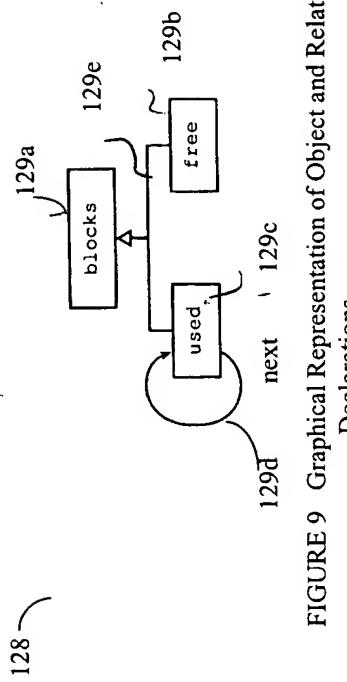


FIGURE 9 Graphical Representation of Object and Relation Declarations

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```
C   :=  Q, C | G ⇒ I
Q   :=  for V in S | for ⟨V, V⟩ in R |
        for V = E .. E
G   :=  G and G | G or G | G | E = E | E < E | true |
        (G) | E in S | ⟨E, E⟩ in R
I   :=  E in S | ⟨E, E⟩ in R
E   :=  V | number | string | E.field |
        E.field[E] | E - E | E + E | E/E | E * E
```

FIGURE 10 Model Definition Language

$hv \in \text{HeapValue} = \text{Bit} \cup \text{Byte} \cup \text{Short} \cup \text{Integer} \cup \text{Struct}$
 $h \in \text{Heap} = \mathcal{P}(\text{Object} \times \text{Field} \times \text{HeapValue}) \cup$
 $\quad \text{Object} \times \text{Field} \times \mathbb{N} \times \text{HeapValue}$
 $v \in \text{Value} = \mathbb{Z} \cup \text{Boolean} \cup \text{string} \cup \text{Struct}$
 $l \in \text{Local} = \text{Var} \rightarrow \text{Value}$
 $s \in \text{Store} = \text{Value} \times \text{Value} \cup \text{Value}$
 $m \in \text{Model} = \mathcal{P}(\text{Var} \times \text{Store})$
 $\mathcal{R} : C \rightarrow \text{Heap} \rightarrow \text{Local} \rightarrow \text{Model} \rightarrow \text{Model}$
 $\mathcal{E} : E \rightarrow \text{Heap} \rightarrow \text{Local} \rightarrow \text{Model} \rightarrow \text{Value}$
 $\mathcal{G} : G \rightarrow \text{Heap} \rightarrow \text{Local} \rightarrow \text{Model} \rightarrow \text{Boolean}$
 $\mathcal{I} : I \rightarrow \text{Heap} \rightarrow \text{Local} \rightarrow \text{Model} \rightarrow \text{Model}$

$\mathcal{R}[\text{for } V \text{ in } S, C] h l m = \bigcup_{n \in m(S)} \mathcal{R}[C] h l[V \mapsto v] m$
 $\mathcal{R}[\text{for } (V_1, V_2) \text{ in } R, C] h l m = \bigcup_{(v_1, v_2) \in m(n)} \mathcal{R}[C] h l[V_1 \mapsto v_1][V_2 \mapsto v_2] m$
 $\mathcal{R}[\text{for } V = E_1 \dots E_2, C] h l m =$
 $\quad \bigcup_{i := \mathcal{E}[E_1] h l m}^{\mathcal{E}[E_2] h l m} \mathcal{R}[C] h l[V \mapsto i] m$
 $\mathcal{R}[C \Rightarrow I] h l m = \text{if } (\mathcal{G}[C] h l m) \text{ then } (\mathcal{I}[I] h l m) \text{ else } m$
 $\mathcal{G}[G_1 \text{ and } G_2] h l m = (\mathcal{G}[G_1] h l m) \wedge (\mathcal{G}[G_2] h l m)$
 $\mathcal{G}[G_1 \text{ or } G_2] h l m = (\mathcal{G}[G_1] h l m) \vee (\mathcal{G}[G_2] h l m)$
 $\mathcal{G}[\neg G] h l m = \neg(\mathcal{G}[G] h l m)$
 $\mathcal{G}[E_1 = E_2] h l m = (\mathcal{E}[E_1] h l m) == (\mathcal{E}[E_2] h l m)$
 $\mathcal{G}[E_1 < E_2] h l m = (\mathcal{E}[E_1] h l m) < (\mathcal{E}[E_2] h l m)$
 $\mathcal{G}[\text{true}] h l m = \text{true}$
 $\mathcal{G}[E \text{ in } S] h l m = \langle S, \mathcal{E}[E] h l m \rangle \in m$
 $\mathcal{G}(E_1, E_2) \text{ in } R] h l m = \langle R, \mathcal{E}[E_1] h l m, \mathcal{E}[E_2] h l m \rangle \in m$
 $\mathcal{I}[E \text{ in } S] h l m = m \cup (S, \mathcal{E}[E] h l m)$
 $\mathcal{I}(E_1, E_2) \text{ in } R] h l m = m \cup \langle R, \langle \mathcal{E}[E_1] h l m, \mathcal{E}[E_2] h l m \rangle \rangle$
 $\mathcal{E}[V] h l m = l(V)$
 $\mathcal{E}[\text{number}] h l m = \text{number}$
 $\mathcal{E}[E, field] h l m = b \text{ such that } ((\mathcal{E}[E] h l m), field, b) \in h$
 $\mathcal{E}[E_1, field(E_2)] h l m =$
 $\quad c, \text{such that } ((\mathcal{E}[E_1] h l m), field, (\mathcal{E}[E_2] h l m), c) \in h$
 $\mathcal{E}[E_1 \oplus E_2] h l m = \text{primop}(\oplus, (\mathcal{E}[E_1] h l m), (\mathcal{E}[E_2] h l m))$
 $\mathcal{E}[\text{string}] h l m = \text{string}$

FIGURE 11 Denotational Semantics for Model Definition Language

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Disk disk;

for i in 0..NumEntries, disk.table[i].valid &&
disk.table[i].first < NumBlocks ==>
disk.table[i].first in used;
for b in used, 0 <= disk.FAT[b] &&
disk.FAT[b] < NumBlocks => disk.FAT[b] in used;
for b in used, 0 <= disk.FAT[b] &&
disk.FAT[b] < NumBlocks ==>
<b,disk.FAT[b]> in next;
for b in 0..NumBlocks, !(b in used) => b in free;

FIGURE 12A Model Definition Declarations and Rules

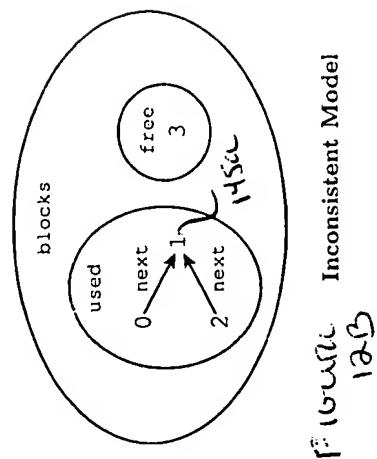
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C := Q, C | B
Q := for V in S | for V = E .. E
B := B and B | B or B | B | (B) |
VE = E | VE < E | VE <= E | VE > E |
VE >= E | V in SE | size(SE) = C |
size(SE) >= C | size(SE) <= C
VE := V.R
E := V | number | string | E + E | E - E | E / E |
E * E | E..R | size(SE) | (E)
SE := S | V.R | R.V

Figure 13 Internal Constraint Language

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$$\begin{aligned}
 v &\in Value = Number \cup Boolean \cup string \cup Object \\
 l &\in Local = \mathcal{P}(Var \times Value) \\
 m &\in Model = \mathcal{P}(Var \times Store) \\
 s &\in Store = Value \times Value \cup Value \\
 \mathcal{E}V &: C \rightarrow Local \rightarrow Model \rightarrow Boolean \\
 \mathcal{E} &: E \rightarrow Local \rightarrow Model \rightarrow Value \\
 C &: B \rightarrow Local \rightarrow Model \rightarrow Boolean \\
 V &: VE \rightarrow Local \rightarrow Model \rightarrow Value \\
 SE &: SE \rightarrow Local \rightarrow Model \rightarrow \mathcal{P}(Value)
 \end{aligned}$$

$$\begin{aligned}
 \mathcal{E}V[\text{for } V \text{ in } S.C] l m &= \\
 \wedge_{v \in m(S)} \mathcal{E}V[C] l[V \mapsto v] m & \\
 \mathcal{E}V[\text{for } V = E_1..E_2, C] l m &= \\
 \wedge_{E=E_1..E_2} \mathcal{E}V[C] l[V \mapsto v] m & \\
 \wedge_{v \in E.l.m} \mathcal{E}V[C] l[V \mapsto v] m & \\
 \mathcal{E}V[B.l.m] &= C[B].l.m \\
 C[B].l.m &= \neg C[B].l.m \\
 C[B_1] \text{ and } C[B_2].l.m &= C[B_1].l.m \wedge C[B_2].l.m \\
 C[B_1] \text{ or } C[B_2].l.m &= C[B_1].l.m \vee C[B_2].l.m \\
 C[V \text{ in } SE].l.m &= l(V) \in SE.l.m \\
 C[V.E = E].l.m &= (V[V.E]).l.m == \mathcal{E}[E].l.m \\
 C[V.E < E].l.m &= (V[V.E]).l.m < \mathcal{E}[E].l.m \\
 C[V.E \leq E].l.m &= (V[V.E]).l.m \leq \mathcal{E}[E].l.m \\
 C[V.E > E].l.m &= (V[V.E]).l.m > \mathcal{E}[E].l.m \\
 C[V.E \geq E].l.m &= (V[V.E]).l.m \geq \mathcal{E}[E].l.m \\
 C.size(SE) &= C.l.m = \mathcal{E}[\text{size}(SE)].l.m == C \\
 C.size(SE) >= C.l.m &= \mathcal{E}[\text{size}(SE)].l.m \geq C \\
 C.size(SE) <= C.l.m &= \mathcal{E}[\text{size}(SE)].l.m \leq C \\
 V[R].l.m &= y \text{ such that } \langle l(V), y \rangle \in m(R) \\
 \mathcal{E}[\text{size}(SE)].l.m &= |\mathcal{E}[SE].l.m| \\
 \mathcal{E}[V].l.m &= l(V) \\
 \mathcal{E}[E.R].l.m &= y \text{ such that } \exists z, z \in \mathcal{E}[E].l.m \wedge \langle z, y \rangle \in m(R) \\
 \mathcal{E}[E_1 \oplus E_2].l.m &= \text{primon}(\oplus, \mathcal{E}[E_1].l.m, \mathcal{E}[E_2].l.m) \\
 SE[S].l.m &= \{s \mid s \in m(S)\} \\
 SE[V.R].l.m &= \{y \mid \langle l(V), y \rangle \in m(R)\} \\
 SE[R.V].l.m &= \{y \mid \langle y, l(V) \rangle \in m(R)\}
 \end{aligned}$$

Fig. 14 Denotational Semantics for Internal Constraint Language

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$R ::= Q, R \mid G \Rightarrow C$
 $Q ::= \text{for } V \text{ in } S \mid \text{for } \langle V, V \rangle \text{ in } R \mid \text{for } V = E .. E$
 $G ::= G \text{ and } G \mid G \text{ or } G \mid G \mid E = E \mid E < E \mid \text{true}$
 $C ::= HE.field = E \mid HE.field[E] = E \mid V = E$
 $HE ::= V \mid HE.field \mid HE.field[E]$
 $E ::= V \mid \text{number} \mid \text{string} \mid E.R \mid E - E \mid E + E \mid$
 $E * E \mid E/E \mid \text{size}(SE) \mid \text{element } E \text{ of } SE$
 $SE ::= S \mid V.R \mid R.V$

F(x)wR₁₅ External Constraint Language

$hv \in HeapValue = Bit \cup Byte \cup Short \cup Integer \cup Struct$
 $h \in Heap = P(Object \times Field \times HeapValue \cup$
 $v \in Value = \mathbb{Z} \cup Boolean \cup string \cup Struct$
 $l \in Local = Var \rightarrow Value$
 $s \in Store = Value \times Value \cup Value$
 $m \in Model = (P)(Var \times Store)$
 $R : R \rightarrow Heap \rightarrow Local \rightarrow Model \rightarrow Boolean$
 $\mathcal{E} : E \rightarrow Heap \rightarrow Local \rightarrow Model \rightarrow Value$
 $\mathcal{HE} : HE \rightarrow Heap \rightarrow Local \rightarrow Model \rightarrow Object$
 $\mathcal{G} : G \rightarrow Heap \rightarrow Local \rightarrow Model \rightarrow Boolean$
 $\mathcal{C} : C \rightarrow Heap \rightarrow Local \rightarrow Model \rightarrow Boolean$
 $\mathcal{SE} : SE \rightarrow Local \rightarrow Model \rightarrow Value$

$\mathcal{R}[for\ V\ in\ S, R|h\ l\ m = \Lambda_{o \in m(S)} \mathcal{R}[R]h|l[V \mapsto v]m]$
 $\mathcal{R}[for\ (V_1, V_2)\ in\ R, R|h\ l\ m = \Lambda_{(v_1, v_2) \in m(R)}$
 $\mathcal{R}[R]h|l[V_1 \mapsto v_1][V_2 \mapsto v_2]m$
 $\mathcal{R}[for\ V = E_1 \dots E_2, R|h\ l\ m = \Lambda_{v \in \mathcal{E}[E_1] h\ l\ m}$
 $\mathcal{R}[R]h|l[V \mapsto v]m$
 $\mathcal{R}[C \Rightarrow C|h\ l\ m = (\neg G[C])h\ l\ m) \vee C[C]h\ l\ m)$
 $G[G_1 \text{ and } G_2]h\ l\ m = (G[G_1]h\ l\ m) \wedge (G[G_2]h\ l\ m)$
 $G[G_1 \text{ or } G_2]h\ l\ m = (G[G_1]h\ l\ m) \vee (G[G_2]h\ l\ m)$
 $G[G_1]h\ l\ m = \neg(G[G_1]h\ l\ m)$
 $G[E_1 < E_2]h\ l\ m = (\mathcal{E}[E_1]h\ l\ m) == (\mathcal{E}[E_2]h\ l\ m)$
 $G[true]h\ l\ m = true$
 $C[HE.field = E]h\ l\ m = (\mathcal{HE}[HE]h\ l\ m, field, \mathcal{E}[E]h\ l\ m) \in h$
 $C[HE.field[E_1] = E_2]h\ l\ m =$
 $(\mathcal{HE}[HE]h\ l\ m, field, \mathcal{E}[E_1]h\ l\ m, \mathcal{E}[E_2]h\ l\ m) \in h$
 $C[V = E]h\ l\ m = (l(V) == \mathcal{E}[E]h\ l\ m)$
 $\mathcal{HE}[HE.field[HE]h\ l\ m = b \text{ such that } (\mathcal{HE}[HE]h\ l\ m, field, b) \in h$
 $\mathcal{HE}[HE.field[HE]h\ l\ m =$
 $b \text{ such that } (\mathcal{HE}[HE]h\ l\ m, field, \mathcal{E}[E]h\ l\ m, b) \in h$
 $\mathcal{E}[V]h\ l\ m = l(V)$
 $\mathcal{E}[number]h\ l\ m = number$
 $\mathcal{E}[V.R]h\ l\ m = b \text{ such that } (V, b) \in m(R)$
 $\mathcal{E}[E_1 \oplus E_2]h\ l\ m = primop(\oplus, (\mathcal{E}[E_1]h\ l\ m), (\mathcal{E}[E_2]h\ l\ m))$
 $\mathcal{E}[string]h\ l\ m = string$
 $\mathcal{E}[size(SE)]h\ l\ m = |\mathcal{SE}[SE]h\ l\ m|$
 $\mathcal{E}[element E \text{ of } SE]h\ l\ m = \mathcal{SE}[SE]h\ l\ m$
 $\mathcal{SE}[S]h\ l\ m = \{s \mid s \in m(S)\}$
 $\mathcal{SE}[V.R]h\ l\ m = \{y \mid \langle \langle V, y \rangle, y \rangle \in R\}$
 $\mathcal{SE}[R.V]h\ l\ m = \{y \mid \langle y, l(V) \rangle \in R\}$

F (Formal Logic Denotational Semantics for External Constraint Language)

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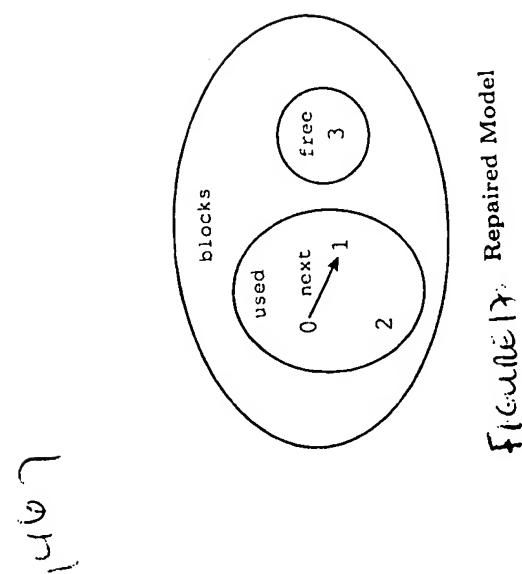


Figure 17: Repaired Model

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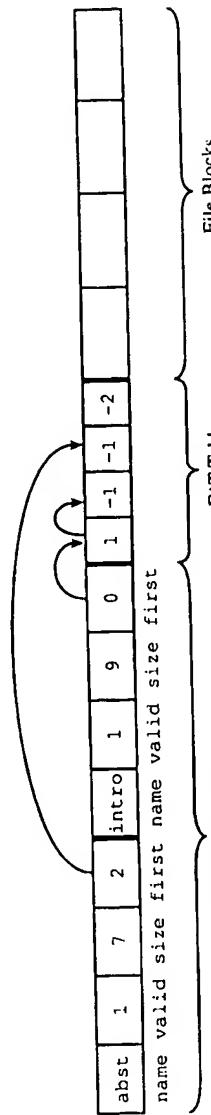


Figure 18 Repaired File System

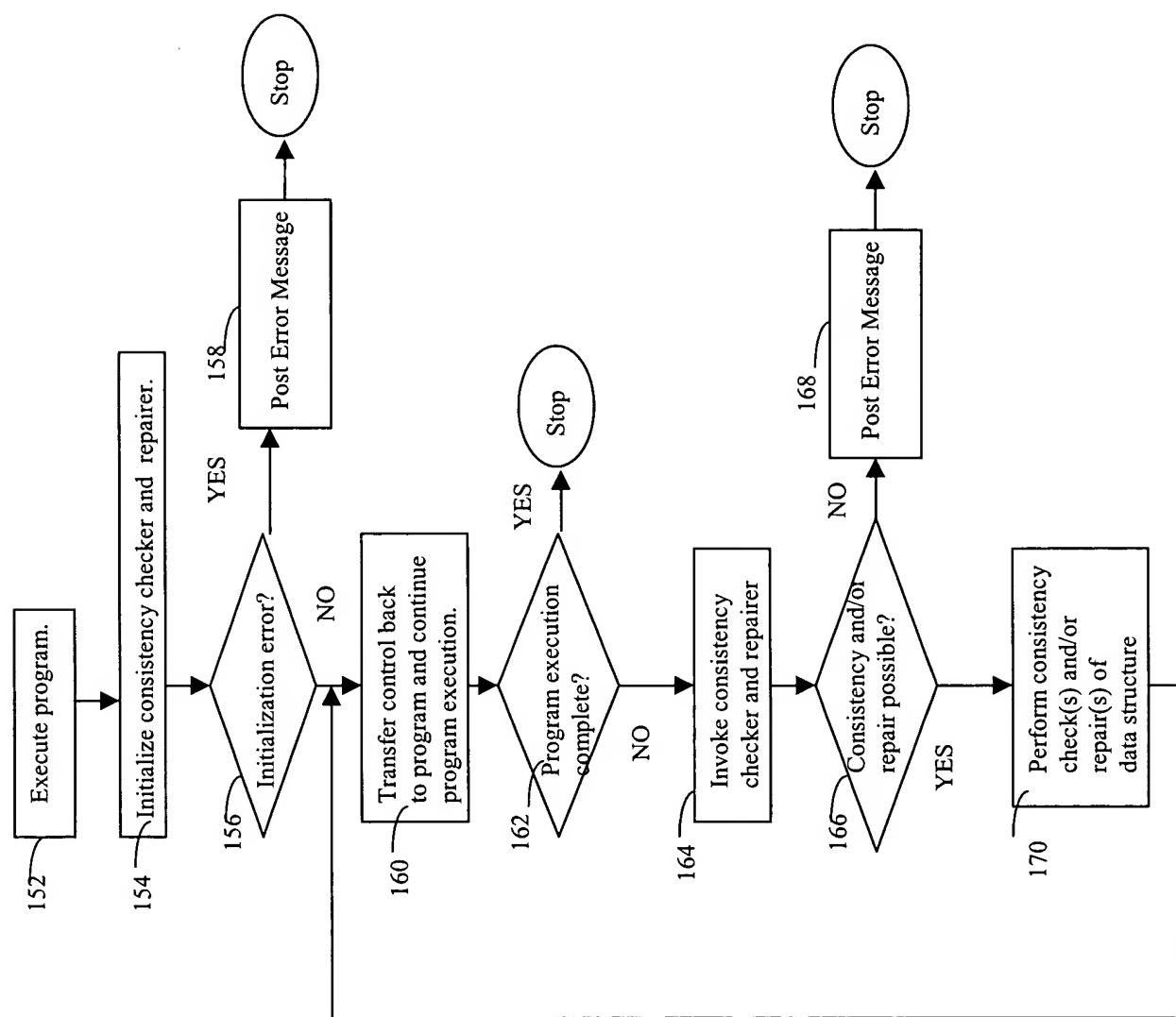
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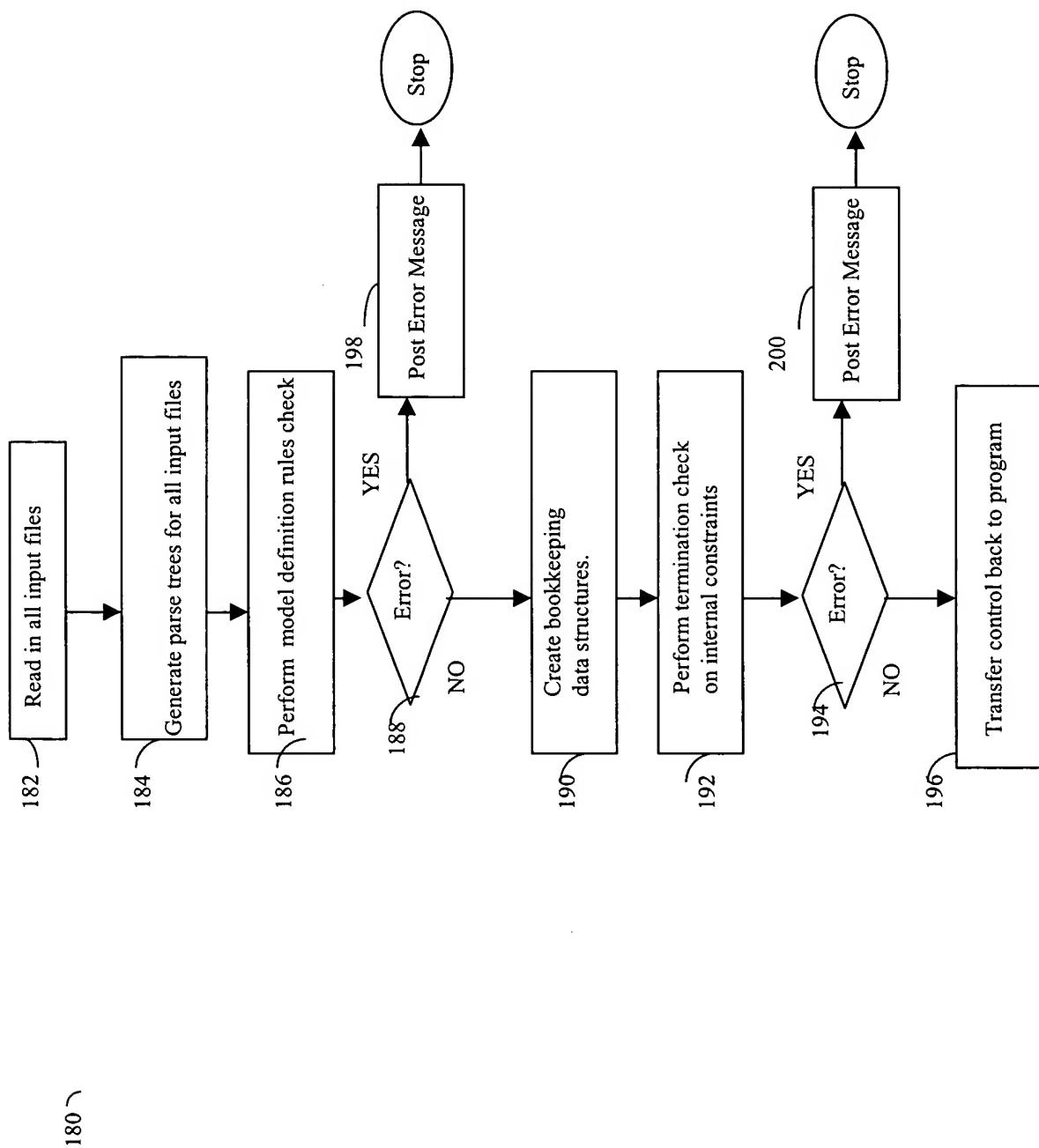


FIGURE 20

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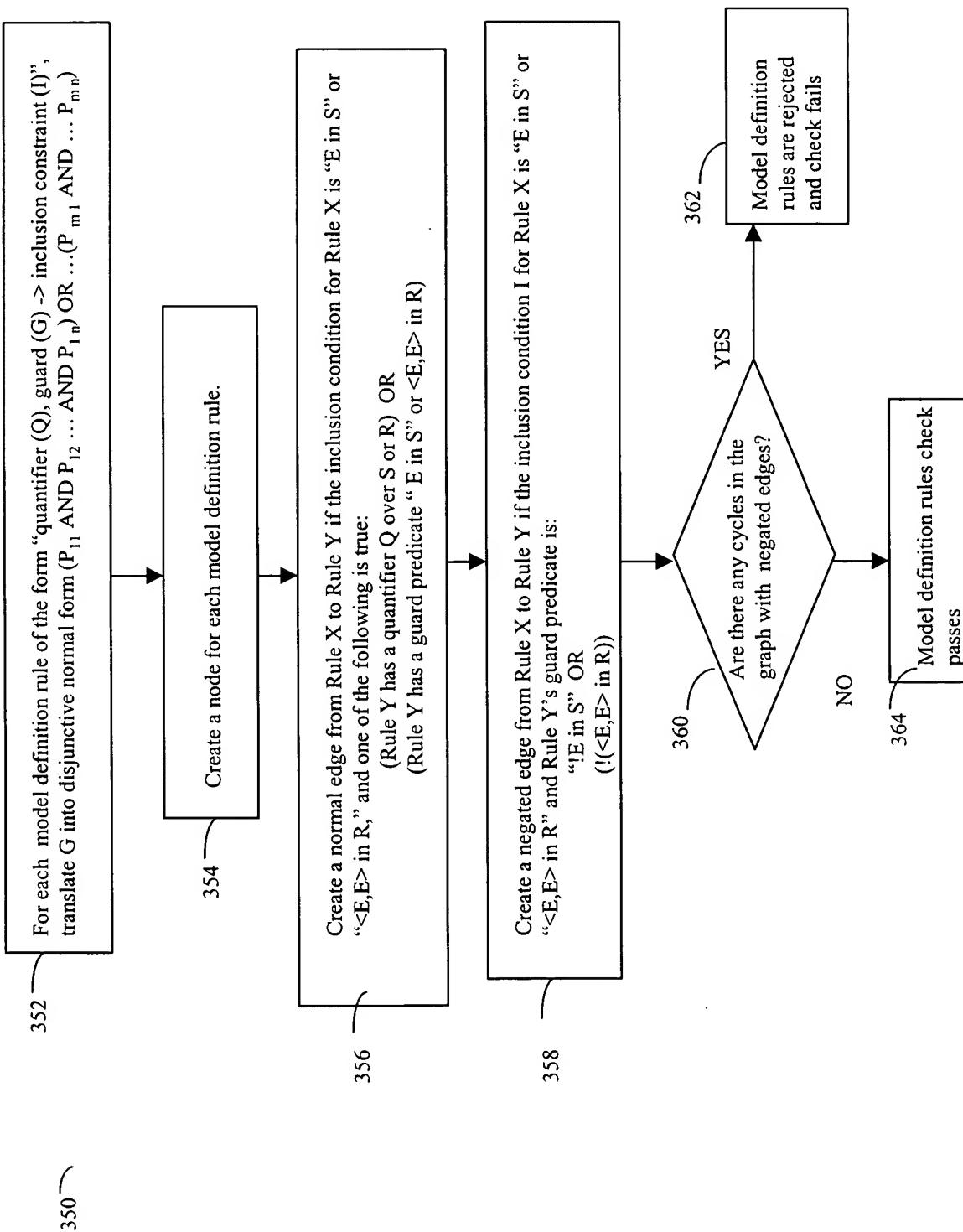


FIGURE 21

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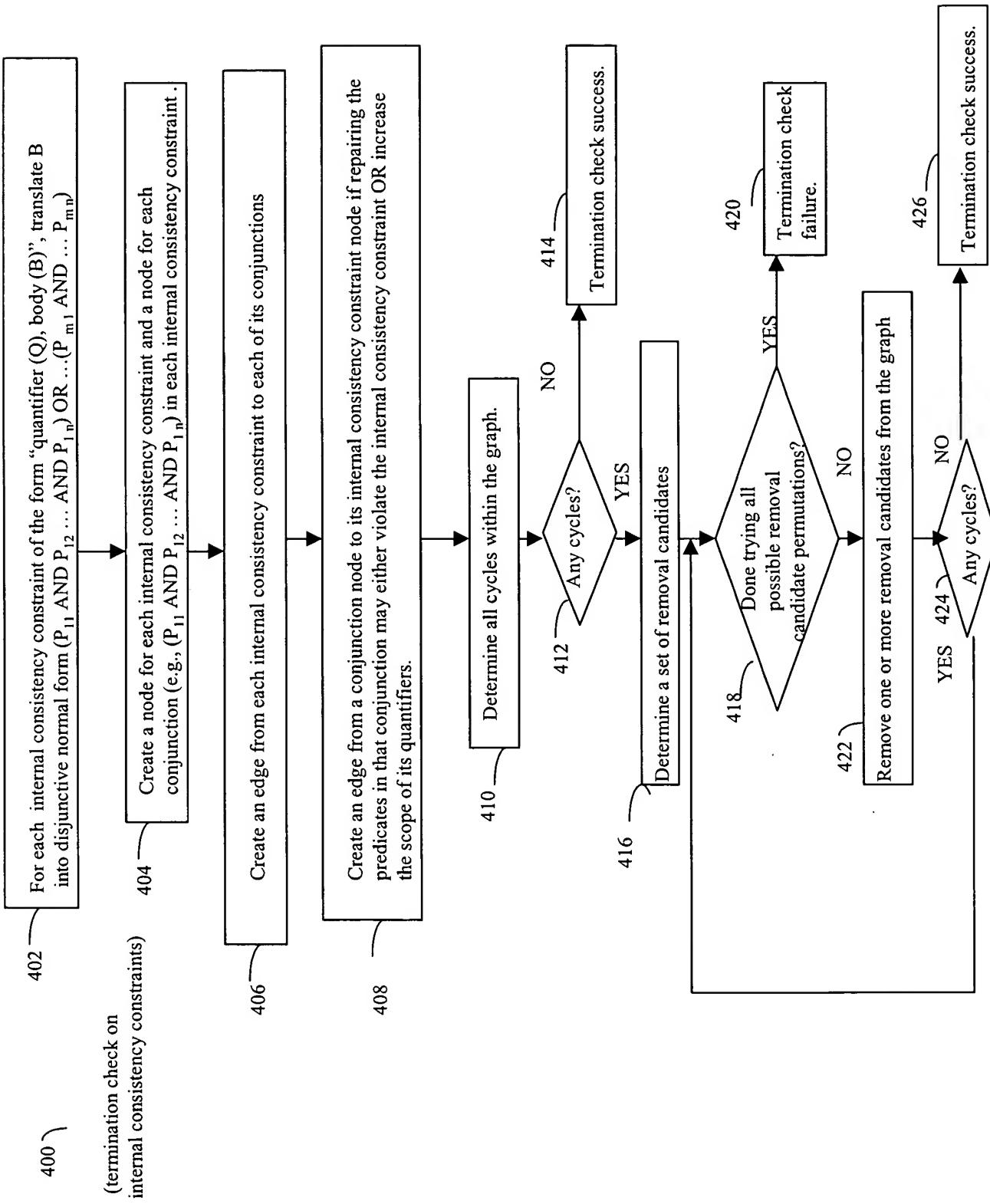


FIGURE 22

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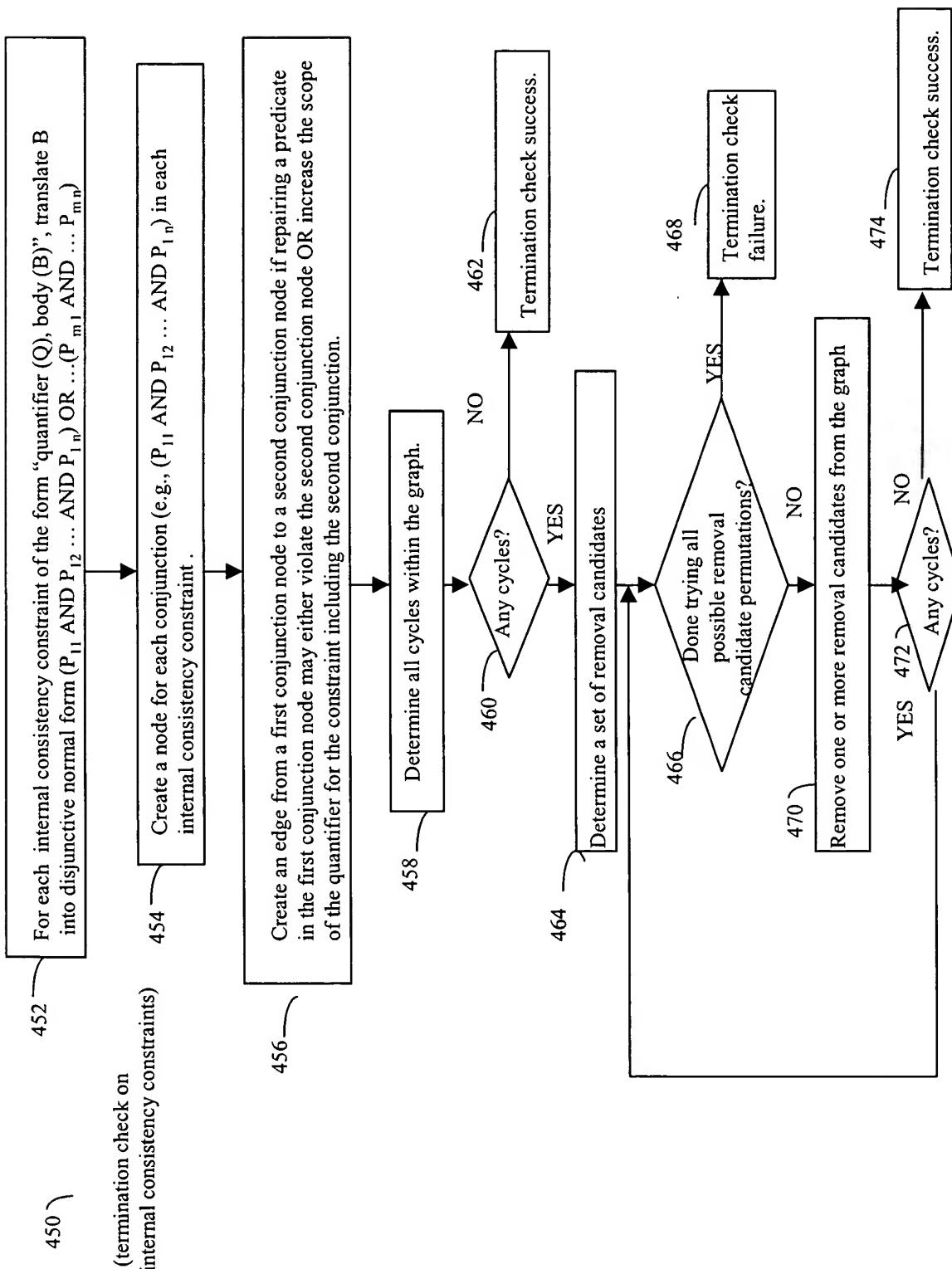


FIGURE 23

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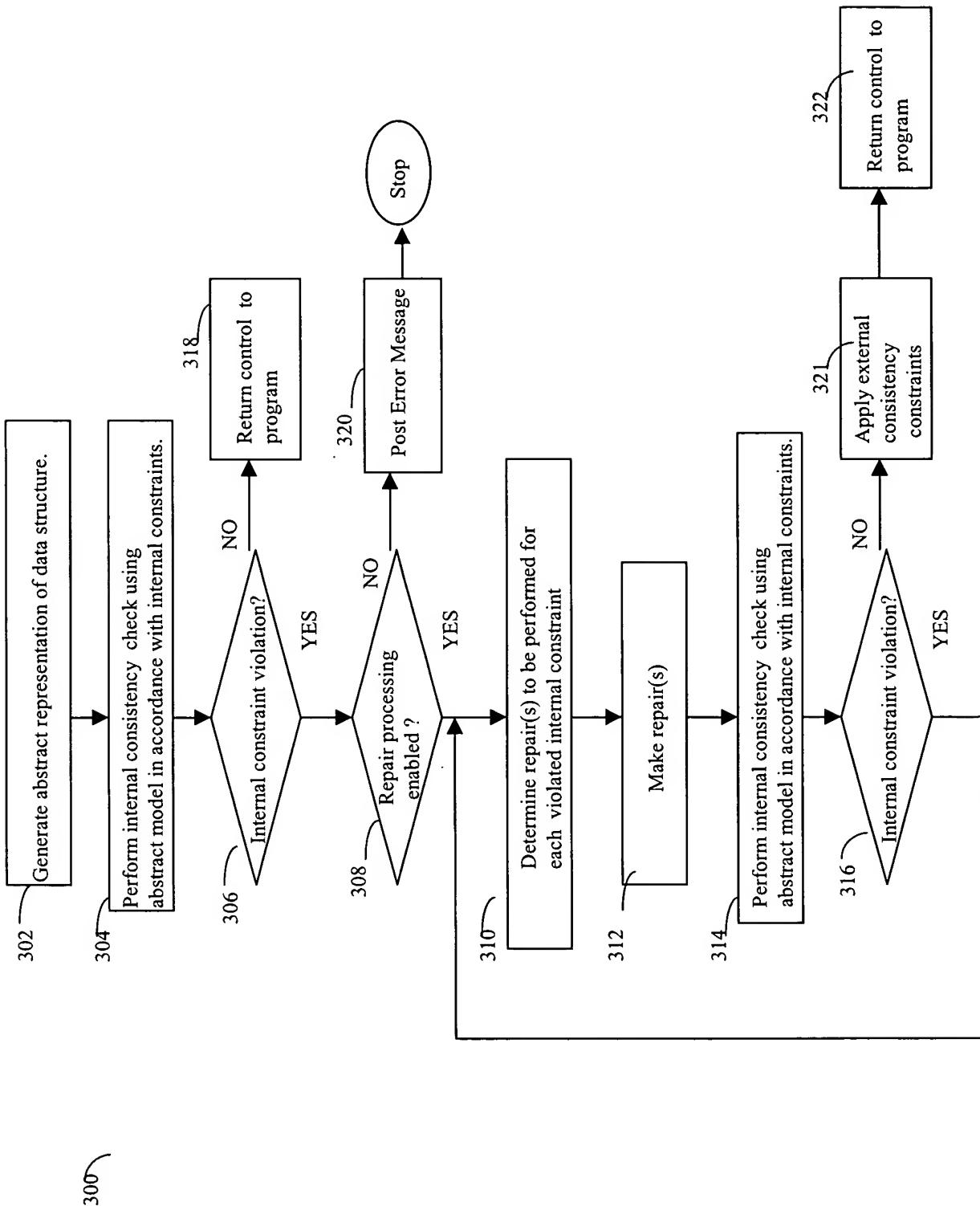


FIGURE 24

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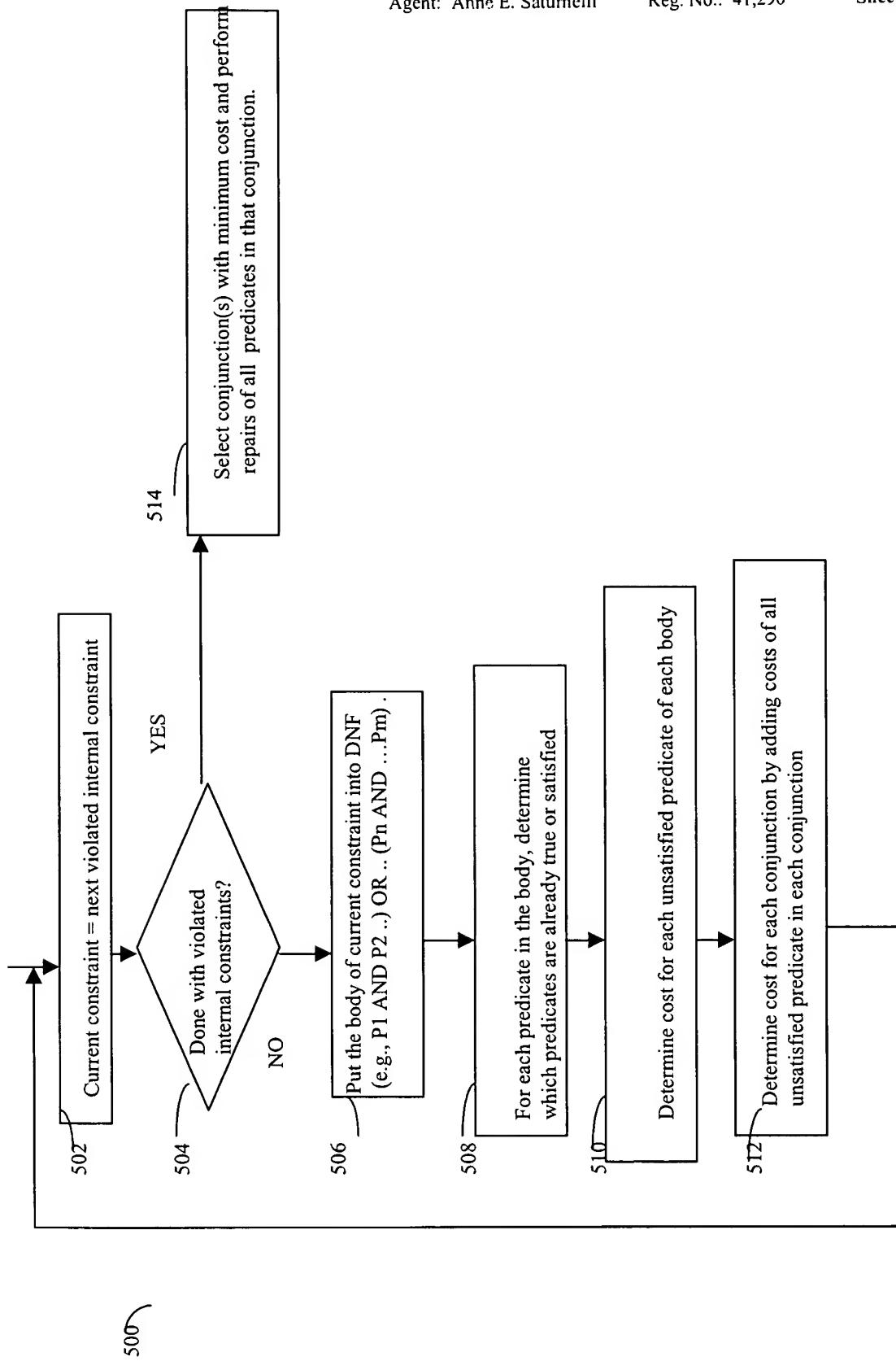


FIGURE 25

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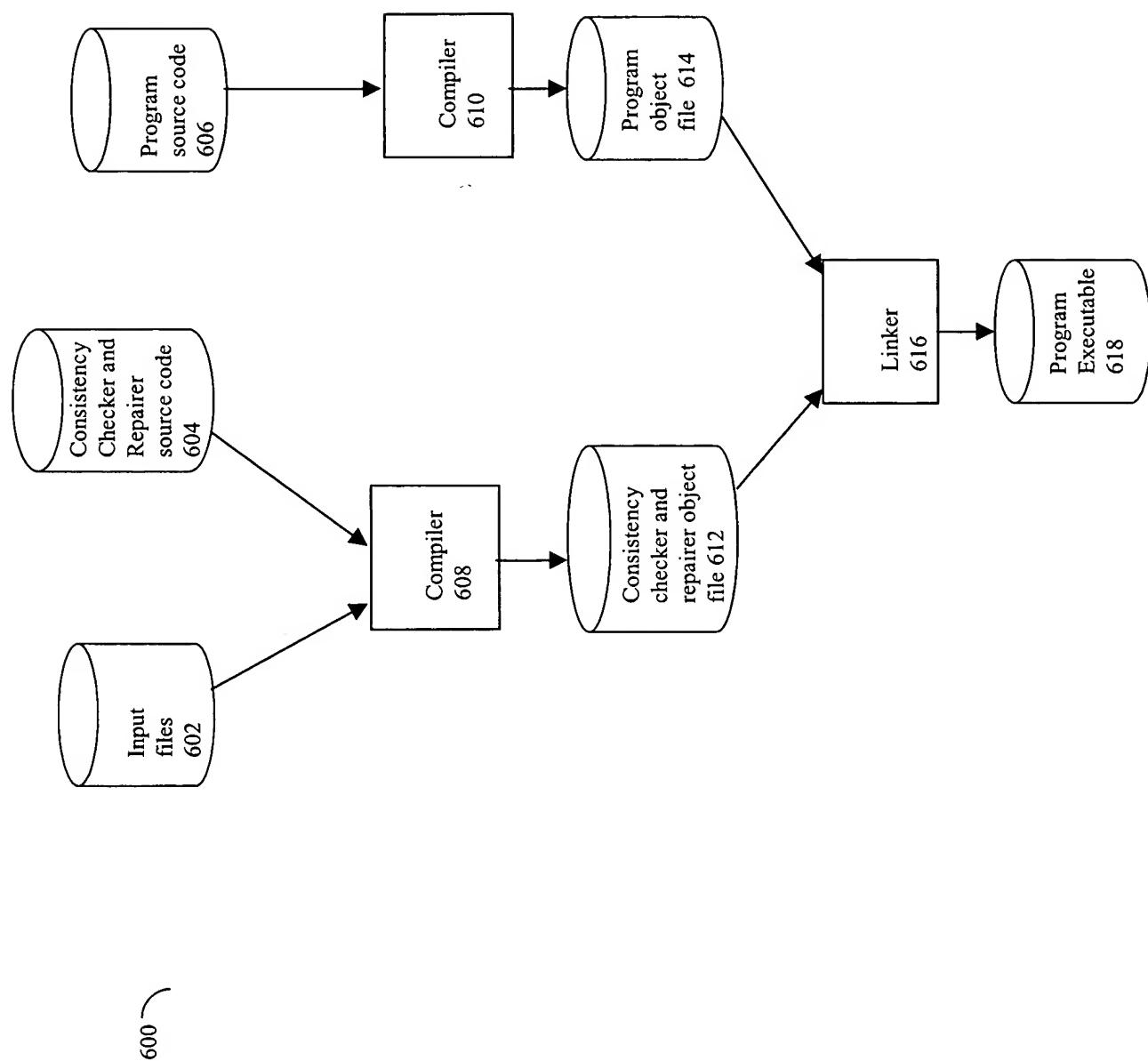


FIGURE 26

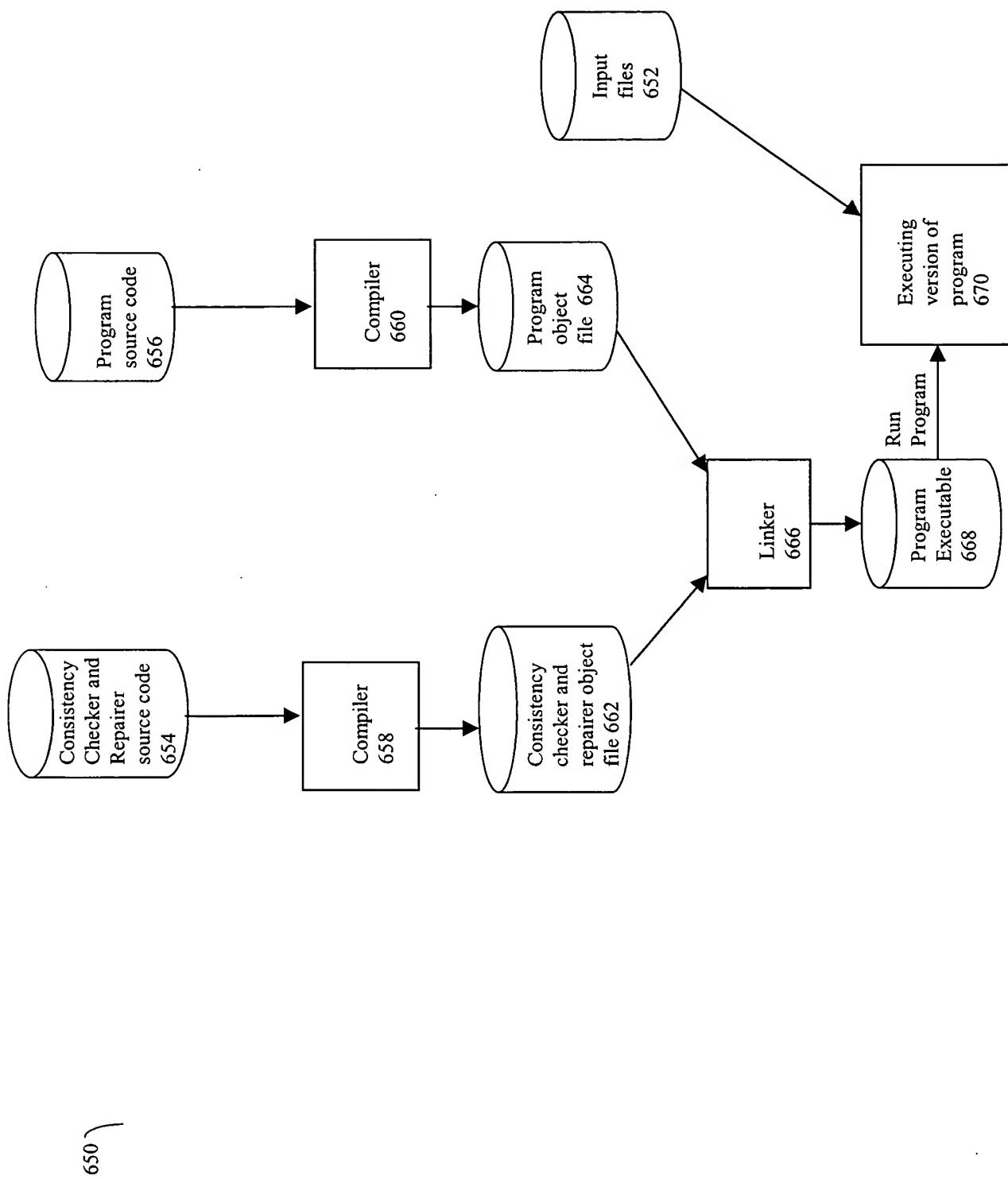


FIGURE 27